

Maths 190 Lecture 13

Question of the day: What is the most symmetric figure you can draw in the plane? What if you can use only straight lines?

A **regular polygon** is a shape in the plane, with the sides being straight line pieces of equal length and with all the interior angles between sides being equal.

How many regular polygons are there?

A variation of the question of the day: What is the most symmetric three-dimensional object? What if all the sides of the object have to be flat?

A **regular solid or polyhedra** is a three-dimensional object with all the surfaces being identical (flat) regular polygons and with the number of edges coming out of a vertex being the same for all vertices.

How many regular solids are there?

Features of the regular solids

| Solid | Vertices | Edges | Faces | Number of Faces per Vertex | Number of Sides per Face |
|--------------|----------|-------|-------|----------------------------|--------------------------|
| Tetrahedron | | | | | |
| Cube | | | | | |
| Octahedron | | | | | |
| Dodecahedron | | | | | |
| Icosahedron | | | | | |

Important ideas from today:

- ▶ There are five regular (or Platonic) solids: the tetrahedron, cube, octahedron, dodecahedon and icosahedron.
- ▶ No other solids can be created with identical, regular polygonal faces meeting together so that the number of edges meeting at any vertex of the solid is the same.
- ▶ There are some interesting relationships between the numbers of edges, vertices and faces for the Platonic solids. For instance, $V - E + F = 2$, where V is the number of vertices, E is the number of edges, and F is the number of faces of a solid.