DEPARTMENT OF MATHEMATICS

- 1. (a) Some go to $+\infty$ and some to $-\infty$.
 - (b) Straight line solution.
 - (c) If $y_0 > -\frac{1}{2}t_0 \frac{1}{4}$, then $y \to +\infty$, otherwise to $-\infty$.
- 2. (a)
 - (b) It will be 1.
 - (c) $y_1 = 1, y_2 = 2.$
 - (d) y(0) = 13.3995 so the error is 11.3995.
 - (e) Effective order tends to 1.
 - (f) Effective order tends to 2 for Improved Euler and to 4 for 4th order Runge-Kutta.
- 3. Using 4th order Runge-Kutta, we see the solution is 7.327 to 3 d.p. This is obtained in 2 steps for Runge-Kutta, approximately 32 steps for Improved Euler and over 512 steps for Euler.